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Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. 2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.



17CS36

(06 Marks)

- b. ABC is an equilateral triangular, whose sides are of length 1 cm each. If we select 5 points inside the triangle, prove that atleast two of these points are such that the distance between then is less than ¹/₂ cm.
- c. Let $A = \{1, 2, 3, 4\}$ and R be a relations on A defined by xRy if and only if "x divides y", written x/y. Write down R as a set of order pairs, draw the diagraph of R and determine indegree and outdegree of the vertices of the graph. (07 Marks)

OR

- 6 a. State pigeon hole principle. A bag contains 12 pairs of socks (each pair in different color). If a person drawn the socks one by one at random, determine atmost how many draws are required to get atleast one pair of matched socks. (05 Marks)
 - b. Let f, g, h be functions from z to z defined by f(x)=x-1, g(x)=3x, $h(x) = \begin{cases} 0 & \text{if } x \text{ is even} \\ 1 & \text{if } x \text{ is odd} \end{cases}$
 - Determine (fo(goh))(x) and ((fog)oh)(x) and verify that fo(goh) = (fog)oh. (07 Marks)
 - c. Let, $R = \{(1, 1), (1, 2), (1, 3), (1, 4), (2, 4), (2, 2), (3, 3), (4, 4)\}$ be relation, verify that R is a partial ordering relation or not. If yes, draw the Hasse diagram for R. (08 Marks)

Module-4

- 7 a. Determine the number of positive integers n such that $1 \le n \le 100$ and n is not divisible by 2, 3 or 5. (07 Marks)
 - b. Find the number of derangements of 1, 2, 3, 4 and list them. (05 Marks)
 - c. The number of virus affected files in a system is 1000 (to start with) and this increases by 250% every two hours. Use a recurrence relation to determine the number of virus affected files in the system after one day? (08 Marks)

OR

- 8 a. In how many ways can the 26 letters of the English alphabet be permuted so that none of the patterns CAR, DOG, FUN or BYTE occurs? (08 Marks)
 - b. An Apple, a Banana, a Mango and an Orange are to be distributed to four boys B₁, B₂, B₃, B₄. The boys B₁ and B₂ do not wish to have Apple, the boy B₃ does not want Banana or Mango and B₄ refuses orange. In how many ways the distribution can be made so that no boy is displeased? (07 Marks)

c.	Solve the recurrence relation	C A	
	$a_n - 6a_{n-1} + 9a_{n-2} = 0$ for $n \ge 2$, given	that $a_0 = 5$, $a_1 = 12$.	(05 Marks)
	Modu	le-5	

	Module e	
9	a. Define Isolated vertex, complete graph, Trail path with example.	(06 Marks)
	b. Explain Konigsberg bridge problem.	(07 Marks)
	c. Using the mergesort method, sort the list	
	7, 3, 8, 4, 5, 10, 6, 2, 9	(07 Marks)

OR

- 10 a. If G(V, E) is a simple graph, prove that $2|E| \le |V|^2 |V|$
 - b. Prove that a tree with n vertices has n 1 edges. (06 Marks)
 - c. Obtain the prefix code represented by the following labeled complete binary tree shown in Fig.Q10(c) and also find the code for the words abc, cdb, bde. (08 Marks)

